

Q- Using mesh analysis determine the current through  $5\Omega$  resistor and voltage  $V$  in the given network.

Let the clockwise currents are  $I_1$  and  $I_2$  as in figure. The current through  $R_3$  will be  $I_1 - I_2$ .

Considering the loop on the left and applying Kirchhoff's law we get

$$\Sigma E = \Sigma IR$$

$$\text{Or } -E_1 + E_3 = I_1(R_1 + R_5) + (I_1 - I_2)R_3$$

$$\text{Or } -4 + 6 = 6I_1 + 1(I_1 - I_2)$$

$$\text{Or } 7I_1 - I_2 = 2 \quad \text{----- (1)}$$

Considering the loop on the right and applying Kirchhoff's law we get

$$\Sigma E = \Sigma IR$$

$$\text{Or } -E_2 - E_3 = I_2(R_4 + R_2) - (I_1 - I_2)R_3$$

$$\text{Or } -15 - 6 = 13I_2 + 1(I_1 - I_2)$$

$$\text{Or } I_1 - 12I_2 = -21 \quad \text{----- (2)}$$

(1)\*12 - (2) gives

$$83I_1 = 45$$

$$\text{Or } I_1 = 45/83 = \mathbf{0.542 \text{ A}}$$

$$\text{And } I_2 = 7I_1 - 2 = 7*0.542 - 2 = \mathbf{1.794 \text{ A}}$$

Hence current through  $5 \text{ W}$  resistor is  $\mathbf{0.542 \text{ A}}$

And the voltage  $V_a$  will be given by considering the central arm as

$$V_a = -E_3 - (I_1 - I_2)R_3 = -6 - (0.542 - 1.794)*1 = \mathbf{-4.748 \text{ V}}$$

