

A capacitor is made from two hollow, coaxial, iron cylinders, one inside the other. The inner cylinder is negatively charged and the outer is positively charged; the magnitude of the charge on each is 10.0 pC. The inner cylinder has a radius of 0.200 mm, the outer one has a radius of 5.40 mm, and the length of each cylinder is 25.0cm.

a) What is the capacitance?

The capacitance of such a capacitor (called a cylindrical capacitor) of length  $L$  is given by

$$C = \frac{2\pi\epsilon_0 L}{\ln(b/a)}$$

Here  $b$  is the radius of the outer cylinder and  $a$  is the radius of the inner cylinder.

Now  $a = 0.200 \text{ mm} = 2.00 \times 10^{-4} \text{ m}$ ;  $b = 5.40 \text{ mm} = 5.40 \times 10^{-3} \text{ m}$

$$L = 25.0 \text{ cm} = 0.250 \text{ m}$$

Substituting in the equation above, we get

$$C = \frac{2\pi\epsilon_0 L}{\ln(b/a)} = \frac{2 \times 3.14 \times 8.854 \times 10^{-12} \times 0.250}{\ln(5.40/0.200)} = \frac{1.39 \times 10^{-11}}{3.30} = 4.22 \times 10^{-12} \text{ F}$$

Or the capacitance of the cylinder is **4.22 pF**.

b) What applied potential difference is necessary to produce these charges on the cylinders?

The charge on the capacitor is related to the potential difference across it as

$$Q = CV$$

Or  $V = Q/C = (10 \text{ pC})/(4.22 \text{ pF}) = \mathbf{2.37 \text{ V}}$ .