

Q1- A proton is released from rest where an electric field of 640 N/C exists. (a) what is the acceleration of proton? (b) how long does it take to reach a speed of 1.2×10^6 m/s (c) How much distance does it travel during this time.

(a) The force experienced by a charge q in the field E is given in magnitude by

$$F = q \cdot E$$

Hence the force experienced by the Proton of charge $q = +e = 1.6 \times 10^{-19}$ C will be

$$F = q \cdot E = 1.6 \times 10^{-19} \cdot 640 = 1.024 \times 10^{-16} \text{ N.}$$

If m is the mass of the proton its acceleration is given by the second law of motion as

$$a = F/m = \frac{1.024 \times 10^{-16} \text{ N}}{1.67 \times 10^{-27} \text{ kg}} = 6.13 \times 10^{10} \text{ m/s}^2.$$

(b) The time taken t to reach the velocity $v = 1.2 \times 10^6$ m/s is given by first equation of motion

$$v = u + a \cdot t$$

where u is the initial velocity ($=0$) and a is the acceleration. Hence

$$1.2 \times 10^6 = 0 + 6.13 \times 10^{10} \cdot t$$

$$\text{Gives } t = \frac{1.2 \times 10^6}{6.13 \times 10^{10}} = 1.96 \times 10^{-5} \text{ s} = 19.6 \mu\text{s}$$

(c) The distance travelled is given by the second equation of motion as

$$s = u \cdot t + \frac{1}{2} a \cdot t^2$$

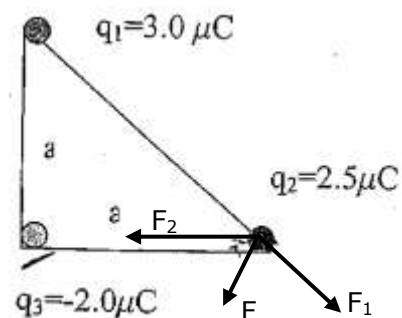
$$\text{or } s = 0 \cdot 1.96 \times 10^{-5} + 0.5 \cdot 6.13 \times 10^{10} \cdot (1.96 \times 10^{-5})^2 = 11.77 \text{ m}$$

4. Consider the following arrangement of charges. Find the total force on the charge q_2 , where $a = 1.0$ m.

The two sides of the triangle are equal, each a and it is a right angled one hence the third side will be $\sqrt{2} \cdot a$ according to Pythagoras theorem and the two equal angles will be 45° each.

The force of attraction or repulsion between two point charges q_1 and q_2 placed at distance ' r ' is given by Coulomb's law and its magnitude is given by

$$F = \frac{1}{4\pi \epsilon_0} \frac{q_1 \cdot q_2}{r^2}$$



Hence the magnitude of the force between charges q_1 and q_2 will be

$$F_1 = \frac{1}{4\pi \epsilon_0} \frac{q_1 \cdot q_2}{r^2} = 9 \times 10^9 \cdot \frac{(3.0 \times 10^{-6}) \cdot (2.5 \times 10^{-6})}{(\sqrt{2} \cdot 1.0)^2} = 3.375 \times 10^{-2} \text{ N}$$

As the two charges are positive both, the force is repulsive as shown in the figure.

Similarly force on charge q_2 due to charge q_3 will be

$$F_2 = \frac{1}{4\pi \epsilon_0} \frac{q_3 * q_2}{r^2} = 9 * 10^9 * \frac{(-2.0 * 10^{-6}) * (2.5 * 10^{-6})}{(1.0)^2} = -4.5 * 10^{-2} N$$

Negative sign shows that it is attractive force.

Hence total force on charge q_2 will be the resultant of F_1 and F_2 and its magnitude is given by

$$F = \sqrt{F_1^2 + F_2^2 + 2F_1F_2 \cos 135^\circ}$$

$$\text{Or } F = \sqrt{(3.375 * 10^{-2})^2 + (4.5 * 10^{-2})^2 + 2 * (3.375 * 10^{-2}) * (4.5 * 10^{-2}) * (-1/\sqrt{2})}$$

$$\text{Or } F = \sqrt{11.4 * 10^{-4} + 20.25 * 10^{-4} - 21.48 * 10^{-4}} = 3.19 * 10^{-2} N$$

And the direction it makes with F_2 is given by

$$\tan \theta = \frac{F_1 \sin 135}{F_2 + F_1 \cos 135} = 1.129$$

$$\text{Or } \theta = 48.5^\circ.$$
