

Q- An aluminum wire having a cross-sectional area of $6.00 \times 10^{-6} \text{ m}^2$ carries a current of 3.70 A. Find the drift-speed of the electrons in the wire. The density of aluminum is 2.70 g/cm^3 . Assume that one conduction electron is supplied by each atom.

The Current density is given by

$$j = n \cdot e \cdot v_d$$

Hence the current will be

$$I = J \cdot A = n \cdot e \cdot v_d \cdot A$$

Here n is the number of free electrons per unit volume.

Hence the drift speed will be

$$v_d = \frac{I}{neA}$$

Now the mass of the unit volume = density

Mass of 1 cm^3 of Al = 2.7 gm

Mass of 1 m^3 of Al = $2.7 \times 10^6 \text{ gm}$

As the molar mass of Al is 26.9815 the number of moles in 1 m^3 of Al will be

$$= 2.7 \times 10^6 / 26.9815 \text{ moles} = 1.0007 \times 10^5 \text{ moles}$$

Hence number of atoms in 1 m^3 of Al = $1.0007 \times 10^5 \times 6.023 \times 10^{23} = 6.027 \times 10^{28}$

As one conduction atom is given by each atom, number of free (conduction) electrons in 1 m^3 will be

$$n = 6.027 \times 10^{28}$$

Thus the drift speed will be

$$v_d = \frac{I}{neA} = \frac{3.70}{(6.027 \times 10^{28}) \times (1.6 \times 10^{-19}) \times 6.00 \times 10^{-6}} = 6.395 \times 10^{-5} \text{ m/s}$$
$$= 6.4 \times 10^{-2} \text{ mm/s}$$