

Q- An aluminum rod has a resistance of 1.234Ω at 20.0°C . Calculate the resistance of the rod at 120°C by accounting for the changes in both the resistivity and its dimensions. (Resistivity of aluminum at 20°C is $2.75 \times 10^{-8} \Omega\text{m}$, temperature coefficient of resistivity is $4.4 \times 10^{-3}/^\circ\text{C}$ and the coefficient of linear expansion of aluminum is $\alpha = 23 \times 10^{-6}/^\circ\text{C}$)

As the temperature coefficient of resistivity if the increase in the resistivity per unit resistivity per degree increase in temperature we may write it as

$$\rho_{coeff} = \frac{\Delta\rho}{\rho \cdot \Delta\theta}$$

Or $\Delta\rho = \rho * \rho_{coeff} * \Delta\theta$

Hence increase in resistivity of aluminum with increase in temperature by $(120 - 20) = 100^\circ\text{C}$ will be

$$\Delta\rho = \rho * 4.4 * 10^{-3} * 100 = 0.44 \rho$$

Hence resistivity at 120°C will be

$$\rho' = \rho + 0.44 \rho = 1.44 \rho$$

Let the length of the rod is L and area of cross section be A at 20°C than resistance of the rod at 20°C will be

$$R = \rho * L / A = 1.234 \Omega \quad \text{----- (1)}$$

Now the coefficient of linear expansion of the aluminum is $\alpha = 23 \times 10^{-6}/^\circ\text{C}$

The new length will be $L + L * \alpha * 100 = L (1.0023)$

As the coefficient of thermal expansion of area $\beta = 2\alpha$, the new area of cross section will be

$$A + A * 2 * \alpha * 100 = A (1.0046)$$

Hence the resistance of the rod at 120°C will be

$$R' = 1.44\rho * L * 1.0023 / (A * 1.0046)$$

Or $R' = (\rho L / A) * 1.44 * 1.0023 / 1.0046$

Or $R' = 1.234 * 1.4367 = 1.7729 \Omega$.