

Q1- A particle moves in simple harmonic motion with a frequency of 1.80 Hz and amplitude of 6.00 cm. What is its maximum speed of the particle?

The maximum speed of a particle in a SHM is given by

$$V_{\max} = A\omega$$

Here A is the amplitude and ω is the angular frequency given by 2π *frequency

Now $\omega = 2\pi$ *frequency = $2*3.14*1.80 = 11.3$ rad/s.

Hence the maximum speed will be

$$V_{\max} = A\omega = (6.00 \text{ cm})*(11.3 \text{ radians/s}) = \mathbf{67.8 \text{ cm/s}}$$

Q2- A transverse wave on a string is described by the following wave function.

$$y = (0.115 \text{ m}) \sin (3.14*x/8 + 12.56 t)$$

(a) Determine the transverse speed and acceleration of an element of the string at $t = 0.280$ s for the point on the string located at $x = 1.80$ m.

$$y = (0.115 \text{ m}) \sin (3.14*x/8 + 12.56 t)$$

So $v(x,t) = dy/dt = (0.115 \text{ m}) \cos (3.14*x/8 + 12.56 t) * 12.56$

Or $v = 12.56 (0.115) \cos (3.14*x/8 + 12.56 t)$ ----- (1)

Substituting the values of x and t in equation (1) we have

$$v = 12.56*0.115*\cos [(3.14*1.80/8)+(4*3.14*0.280)]$$

Or $v = 1.44 \cos (4.22 \text{ rad}) = 1.44*\cos 242.1^\circ$

Or $\mathbf{v = - 0.674 \text{ m/s}}$

And the acceleration is given by

$$a = dv/dt = 12.56 (0.115 \text{ m}) [- \sin (3.14*x/8 + 12.56 t)] *12.54 \text{ using equation (1)}$$

Or $a = - 157.7 (0.115 \text{ m}) \sin (3.14*x/8 + 12.56 t)$ ----- (2)

Substituting the values in equation 2 we get

$$a = - 157.7*0.115 \sin (4.22 \text{ rad})$$

Or $a = - 18.1 \sin 242.1^\circ = 16 \text{ m/s}^2$.

(b) What are the wavelength, period, and speed of propagation of this wave?

The general form of transverse wave equation is given by

$$y = A \sin (kx - \omega t)$$

Here K is the wave constant given by $k = 2\pi/\lambda$ and ω is angular frequency.

Thus comparing with our wave equation

the force constant $k = 2\pi/\lambda = 3.14/8$ Gives $\lambda = 16 \text{ m}$

And angular frequency $\omega = 12.56$ Gives period $T = 2\pi/\omega = 1/2 \text{ sec}$.

And the speed of propagation $c = \lambda/T = 32 \text{ m/s}$