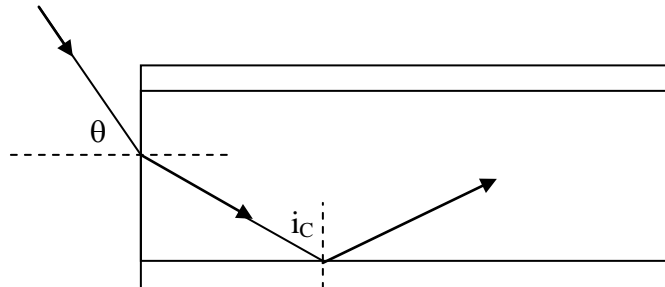


Q- Find the maximum angle of incidence θ_1 of a ray on the plane surface that would propagate through an optical fiber that has a core index of refraction of 1.499, a core radius of $44.00 \mu\text{m}$, and a cladding index 1.496.

The optical fiber is based on the principle of total internal reflection. When light goes from denser to rarer medium and the angle of incidence is greater than critical angle the light is reflected totally and come back the same denser medium. Hence the minimum angle of incidence on the core cladding interface must be the critical angle i_c and the maximum angle of incidence θ must be such that the angle of refraction r at the end of the fiber is $90^\circ - i_c$



Now the critical angle at an interface is given by

$$\sin i_c = \frac{\text{refractive index of rarer medium}}{\text{refractive index of denser medium}} = \frac{1.496}{1.499} = 0.998$$

Gives $i_c = 86.4^\circ$

And hence $r = 90^\circ - 86.4^\circ = 3.6^\circ$

And hence the angle of incidence θ is given by

$$\mu = \frac{\sin \theta}{\sin r}$$

Or $1.499 = \frac{\sin \theta}{\sin 3.6^\circ}$

Or $\sin \theta = 1.499 * \sin 3.6^\circ = 1.499 * 0.0628 = 0.0941$

Gives $\theta = 5.4^\circ$