

Q- A baseball is hit into the air at an initial speed of 30 m/s and an angle of 60° above the horizontal. At the same time, the center fielder starts running towards the batter and catches the ball 1 m above the level at which it was hit. If the center fielder is initially 1.25 x 10<sup>2</sup> m from home plate, what must be his average speed?

Let the time of the flight be t.

Horizontal velocity (constant) of the ball

$$v_x = 30 \cdot \cos(60^\circ) = 30 \cdot 0.50 = 15 \text{ m/s}$$

Initial vertical velocity of the ball

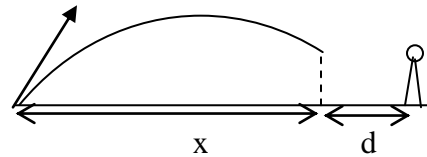
$$v_y = 30 \cdot \sin(60^\circ) = 30 \cdot 0.866 = 26 \text{ m/s}$$

Vertical displacement is given by the second equation of motion as

$$[s = u \cdot t + \frac{1}{2} a \cdot t^2]$$

$$1 = 26 \cdot t + 0.5 \cdot (-9.8) \cdot t^2$$

$$\text{Or } 4.9 \cdot t^2 - 26 \cdot t + 1 = 0$$



$$\text{Gives } t = \frac{26 \pm \sqrt{26^2 - 4 \cdot 4.9 \cdot 1}}{2 \cdot 4.9} = t = \frac{26.38 \pm \sqrt{(26.38)^2 - 4 \cdot 4.9 \cdot 0.958}}{2 \cdot 4.9}$$

$$\text{Or } t = \frac{26 \pm 25.6}{9.8} \quad t = \frac{26.38 \pm 26.02}{9.8}$$

$$\text{Gives } t = 5.267\text{s or } 0.04\text{s}$$

Clearly the time of flight is the one for which the ball coming down and is 5.267s

Hence the horizontal distance covered by the ball in this time will be

$$x = v_x \cdot t = 15 \cdot 5.267 = 79 \text{ m}$$

Thus the distance to be covered by the fielder will be  $d = 125 - 79 = 46 \text{ m}$

Hence the minimum speed of the catcher should be

$$v = d/t = 46/5.267 = \mathbf{8.73 \text{ m/s.}}$$