

Q- A 20V battery has an internal resistance  $r = 2 \text{ ohms}$ . Design a voltage divider supplying 5V (Open circuit) from the end-points of resistor  $R_2 = 10 \text{ ohms}$ . Find the load current when  $R_L = 15 \text{ ohms}$  is connected to the  $R_2$  of the divider and the voltage under load.

When the load resistance is not connected the  $r$ ,  $R_1$  and  $R_2$  are in series with the battery and the total resistance will be

$$R = r + R_1 + R_2$$

The current in the circuit will be

$$I = \frac{V}{r + R_1 + R_2}$$

The potential difference across  $R_2$  will be according to Ohm's law

$$V_2 = I * R_2 = \frac{V * R_2}{r + R_1 + R_2}$$

Substituting the values in above equation we have

$$5 = \frac{20 * 10}{2 + R_1 + 10}$$

$$\text{Or } R_1 = (200 - 60)/5 = \mathbf{28 \Omega}$$

Now when the load is connected parallel to  $10 \Omega$  resistance, the equivalent resistance of the combination will be

$$R' = \frac{R_2 * R_L}{R_2 + R_L} = \frac{10 * 15}{10 + 15} = 6 \Omega$$

Now this resistance is in series with  $R_1$  and  $r$  hence the total resistance of the circuit will be

$$R = R_1 + R' + r$$

$$\text{Or } R = 28 + 6 + 2 = 36 \Omega$$

Hence the current through the battery in this case will be

$$I_1 = 20/36 \text{ A}$$

Thus potential difference across the parallel combination of  $R_2$  and  $R_L$  will be given by the loop rule as

$$\begin{aligned} V &= V_L + (R_1 + r) * I_1 \\ \text{Or } 20 &= V_L + (28 + 2) * (20/36) \end{aligned}$$

$$\text{Gives } V_L = 20 - 16.667 = 3.333 \text{ V}$$

Hence current through the load will be

$$I_L = V_L / R_L = 3.333/15 = 0.222 \text{ A}$$

