Q- A solid cube of silver (density = 10.5 g/ cm^3) has a mass of 90.0 g. (a) What is the resistance between opposite faces of the cube?

Volume of the cube will be = mass/density = 90.0/10.5 = 8.57 cm³. Hence side of the cube L = $(8.57)^{\frac{1}{3}} = 2.05$ cm = 0.0205 m

Resistance of a conductor is given by

$$\mathsf{R} = \frac{\rho L}{A}$$

Where ρ is the resistivity, L is the length and A is area of cross section. The resistivity of silver is 1.62*10⁻⁸ Ωm hence

$$R = \frac{\rho L}{A} = \frac{\rho L}{L^2} = \frac{\rho}{L} = \frac{1.62 \times 10^{-8}}{0.0205} = 7.90 \times 10^{-7} \Omega$$

(b) Assume each silver atom contributes one conduction electron. Find the average drift speed of electrons when a. potential difference of $1.00*10^{-5}$ V is applied to opposite faces. The atomic number of silver is 47, and its molar mass is 107.87 g/mol.

With this applied voltage the current in the cube is given by

$$I = V/R = 1*10^{-5}/(7.90*10^{-7}) = 12.658 A$$

And the current density

$$j = I/A = I/L^2 = 12.658/(0.0205)^2 = 30120 A/m^2$$
 ------ (1)

Now the molar mass of silver is 107.87 gram/mol Hence the number of moles in 10.5 gm i.e. 1 cm^3 will be

$$= 10.5/107.87 = 9.734*10^{-2} \text{ mole/cm}^{3}$$

Hence number of moles per m^3 will be = $9.734*10^4$ mole/ m^3

And hence the number of atoms or conduction electrons per cubic meter will be

$$n = 9.734^{*}10^{4} \times 6.023^{*}10^{23} = 5.863^{*}10^{28}$$

Now the drift velocity is given by

$$vd = j/(n*e)$$

Where n is the number of charge carriers per unit volume

Hence substituting the values we have

$$v_d = \frac{30120}{5.863 \times 10^{28} \times 1.6 \times 10^{-19}} = 3.21 \times 10^{-6} \text{ m/s}$$