

Q- A distant galaxy is simultaneously rotating and receding from the earth. As the drawing shows, the galactic center is receding from the earth at a relative speed of  $u_G = 1.8 \times 10^6$  m/s. Relative to the center, the tangential speed is  $v_T = 0.3 \times 10^6$  m/s for locations  $A$  and  $B$ , which are equidistant from the center. When the frequencies of the light coming from regions  $A$  and  $B$  are measured on earth, they are not the same and each is different than the emitted frequency of  $6.400 \times 10^{14}$  Hz. Find the measured frequency for the light from each of the following.

- (a) region  $A$   
 (b) region  $B$

The frequency of light from a moving source is not as that of the actual one but apparent and given by Doppler's formula for approaching source

$$n' = n \left( \frac{c}{c - v} \right)$$

If the source is receding away it is

$$n' = n \left( \frac{c}{c + v} \right)$$

Here  $c$  is the speed of light and  $v$  is the velocity of approach of the source

- (a) For point  $A$  which is moving away with resultant velocity  $u - v$  we have

$$n_1 = n \left( \frac{c}{c + (u - v)} \right) = 6.4 \times 10^{14} \left( \frac{3 \times 10^8}{3 \times 10^8 + (1.8 - 0.3) \times 10^6} \right) = 6.3682 \times 10^{14} \text{ Hz}$$

- (b) And as the region  $B$  is receding away with a velocity  $v + u$  we have

$$n_2 = n \left( \frac{c}{c + (u + v)} \right) = 6.4 \times 10^{14} \left( \frac{3 \times 10^8}{3 \times 10^8 + (1.8 + 0.3) \times 10^6} \right) = 6.3555 \times 10^{14} \text{ Hz}$$

