

Q- The sun radiates electromagnetic energy at a constant rate of  $3.92 \times 10^{26}$  W.

(a) What is the change in the sun's mass during each second due to radiating energy?

(b) The mass of the sun is  $1.99 \times 10^{30}$  kg. What fraction of the sun's mass is lost during a human lifetime of 75 years?

a) As W (watt) is SI unit of power, which is J/s, the energy radiated by the sun per second is given by

$$\frac{dE}{dt} = 3.92 \times 10^{26} \text{ J}$$

Now according to mass energy relation of Einstein  $E = mc^2$ . Thus loss in mass per second is equal to the loss in energy per second and given by

$$\frac{dm}{dt} = \frac{1}{c^2} \frac{dE}{dt} = \frac{3.92 \times 10^{26}}{(3.0 \times 10^8)^2} = 4.356 \times 10^9 \text{ kg/s}$$

Thus the mass converting per sec in energy i.e. decrease in mass of the sun per second is  $4.356 \times 10^9$  kg/s

b) The mass of the sun converting as energy in 75 years is given by

$$\text{mass} = \text{rate of decrease} \times \text{time}$$

$$\text{or } m = \frac{dm}{dt} \times \Delta t = 4.356 \times 10^9 \times (75 \times 365 \times 86400) = 1.030 \times 10^{19} \text{ kg}$$

And thus the fraction is given by

$$f = \frac{m}{M_s} = \frac{1.030 \times 10^{19}}{1.99 \times 10^{30}} = 5.177 \times 10^{-12}$$