

Q- Two charges Q_c and $-Q_c$ ($Q_c = 4 \mu\text{C}$) are fixed on the x-axis at $x = -6 \text{ cm}$ and $x = 6 \text{ cm}$, respectively. A third charge $Q_b = 5 \mu\text{C}$ is fixed at the origin. A particle with charge $q = 0.5 \mu\text{C}$ and mass $m = 6 \text{ g}$ is placed on the y-axis at $y = 14 \text{ cm}$ and released. There is no gravity. Calculate the initial acceleration of the particle.

The two equal and opposite charges Q_c and $-Q_c$ will make a dipole and the field on the perpendicular bisector of this dipole at a distance y is given by

$$\vec{E}_1 = \frac{1}{4\pi \epsilon_0} \cdot \frac{2Q_c x}{[y^2 + x^2]^{3/2}} \hat{i} = \frac{(9 * 10^9) * 2 * 4 * 10^{-6} * 0.06}{[0.14^2 + 0.06^2]^{3/2}} \hat{i}$$

Or $\vec{E}_1 = 1.22 * 10^6 \hat{i} \text{ N/C}$

Field at the same point due to charge Q_b will be given by Coulomb's law as

$$\vec{E}_2 = \frac{Q_b}{4\pi \epsilon_0 y^2} (\hat{j}) = \frac{(9 * 10^9) * 5 * 10^{-6}}{0.14^2} (\hat{j}) = 2.296 * 10^6 (\hat{j}) \text{ N/C}$$

Hence force on the particle in x direction will be

$$F_x = E_x * q = E_1 * q = 1.22 * 10^6 * 0.5 * 10^{-6} = 0.61 \text{ N}$$

And the force in y direction will be

$$F_y = E_y * q = E_2 * q = 2.296 * 10^6 * 0.5 * 10^{-6} = 1.148 \text{ N}$$

Thus the resultant force on the particle at initial position is given by

$$F = \sqrt{F_x^2 + F_y^2} = \sqrt{0.61^2 + 1.148^2} = 1.3 \text{ N}$$

So the initial acceleration of the particle will be

$$a = \frac{F}{m} = \frac{1.3}{0.006} = 2.17 * 10^2 \text{ m/s}$$

