

Q- Six point charges, four positive (+q) and two negative (-q), are fixed at the positions shown in the x-y plane; $q = 2 \times 10^{-6}$ C and $a = 0.88$ m. A test charge $Q = 1.5 \times 10^{-6}$ C is at the origin. Find the x- and y-components of the total force on Q.

The force on Q due to two +q charges on the y axis will be equal in magnitude and opposite in direction hence will result in zero.

The magnitude of the force due to the two charges on the x axis will be equal and given by

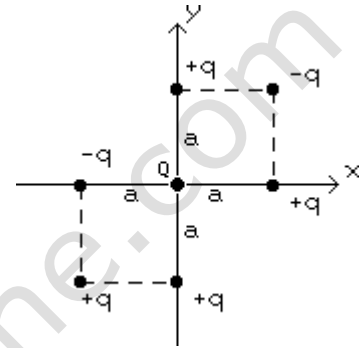
$$\frac{Qq}{4\pi\epsilon_0 a^2}$$

As the force due to +q is repulsive and that due to -q is attractive, both will be in the same - x direction and hence their resultant is given by

$$\vec{F}_1 = 2 * \frac{Qq}{4\pi\epsilon_0 a^2} (-\hat{i})$$

The distance of Q from both the rest two charges on the line bisecting the angle between the axes is equal to $a\sqrt{2}$ and these two charges exerts forces equal in magnitude given by

$$\frac{Qq}{4\pi\epsilon_0 2a^2}$$



As the +q will repel Q and -q will attract Q, the direction of both force will make 45° with x axis and hence magnitude of their resultant is given by

$$F_2 = 2 * \frac{Qq}{4\pi\epsilon_0 2a^2} = \frac{Qq}{4\pi\epsilon_0 a^2}$$

This force can be written in component form as

$$\vec{F}_2 = \frac{Qq}{4\pi\epsilon_0 a^2} (\cos 45^\circ \hat{i} + \sin 45^\circ \hat{j}) = \frac{Qq}{4\sqrt{2} * \pi\epsilon_0 a^2} (\hat{i} + \hat{j})$$

Hence the resultant of the all forces on Q will be given by

$$\vec{F} = \vec{F}_1 + \vec{F}_2 = 2 * \frac{Qq}{4\pi\epsilon_0 a^2} (-\hat{i}) + \frac{Qq}{4\sqrt{2} * \pi\epsilon_0 a^2} (\hat{i} + \hat{j})$$

$$\text{Or } \vec{F} = \frac{Qq}{4\pi\epsilon_0 a^2} \left[2(-\hat{i}) + \frac{1}{\sqrt{2}}(\hat{i} + \hat{j}) \right]$$

$$\text{Or } \vec{F} = \frac{Qq}{4\pi\epsilon_0 a^2} \left[\left(-2 + \frac{1}{\sqrt{2}} \right) \hat{i} + \frac{1}{\sqrt{2}} \hat{j} \right]$$

$$\text{Or } \vec{F} = \frac{(9 * 10^9)(2 * 10^{-6})(1.5 * 10^{-6})}{0.88^2} [-1.293 * \hat{i} + 0.71 \hat{j}]$$

$$\text{Or } \vec{F} = 0.0349 * [-1.293 * \hat{i} + 0.71 * \hat{j}] = -0.045 * \hat{i} + 0.025 * \hat{j}$$

$$\mathbf{F_x = - 0.045 N}$$

$$\mathbf{F_y = 0.025 N}$$