

Q- Figure shows a snapshot graph at  $t = 0$  s of a 30.0 Hz wave traveling to the left. Each interval on the vertical axis corresponds to 5 mm.

From the graph, we get

$$A = \text{two vertical intervals} = 2 \times 5 \text{ mm} = 10 \text{ mm}$$

The wavelength is the distance between two nearest points oscillating in same phase and is equal to

$$\lambda = \text{two horizontal intervals} = 2 \times 1 \text{ m} = 2 \text{ m}$$

(a) What is the wave speed?

The wave speed is given by

$$C = n \times \lambda = 30 \times 2 = \mathbf{60 \text{ m/s}}$$

(b) What is the phase constant of the wave?

The wave displacement of any particle of the medium is given by the equation

$$D = A \sin (kx + \omega t + \phi)$$

From the graph, at  $t = 0$  and  $x = 0$  the displacement of the particle is one vertical interval or  $A/2$ . Hence, we have

$$A/2 = A \sin (0 + 0 + \phi)$$

Gives the phase constant  $\phi = \sin^{-1}(1/2) = 30^\circ$  or  $\pi/6 = 0.5236 \text{ rad}$

(c) Write the displacement equation for this wave. Use "x" for x and "m" for meters.

As we know that

$$K = 2\pi / \lambda = 2\pi / 2 = 3.14 \text{ m}^{-1}$$

$$\text{And } \omega = 2\pi / T = 2\pi \times n = 2 \times 3.14 \times 30 = 188.4 \text{ rad/s}$$

Thus, the equation for the wave can be written as

$$D(x, t) = A \sin (Kx + \omega t + \phi)$$

Substituting the values, we get the equation for the wave as

$$D(x, t) = (10 \text{ mm}) \sin (3.14 x + 188.4 t + 0.5236)$$

