

**Q- A** vertically polarized radio wave of frequency  $9.0 \times 10^5$  Hz traveling into the page. The maximum electric field strength is 1250 V/m.

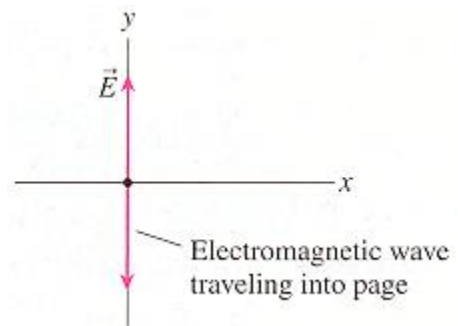
(a) What is the maximum magnetic field strength?

The relation between electric and magnetic field in an electromagnetic field is given by

$$E = cB$$

$$\text{Hence } B_{\max} = E_{\max}/c = 1250/(3 \times 10^8)$$

$$\text{Or } E_{\max} = 4.17 \times 10^{-6} \text{ T}$$



(b) What is the magnetic field strength and direction at a point where  $\vec{E} = (625 \text{ V/m, down})$ ?

Again, using the same formula, the magnitude of the magnetic field is given by

$$B = E/c = 625/(3 \times 10^8) = 2.08 \times 10^{-6} \text{ T}$$

As the direction of the energy transport (Poynting vector) is in to the page and is given in terms of cross product of E and B ( $E \times B$ ) according to the right-hand rule the magnetic field must be in negative x direction or to the left if E is downwards.

(c) What is the smallest distance between a point on the wave having the magnetic field of part b and a point where the magnetic field is at maximum strength?

If at  $t=0$  and  $x=0$ ; E is maximum then the equation of the electric field is given by

$$E = E_{\max} \cos(kx - \omega t)$$

Hence the distance x of the point where E is 625 V/m at  $t = 0$  from origin (where E is maximum at  $t = 0$ ) is given by

$$625 = 1250 \cos(kx - \omega 0)$$

$$\text{Or } \cos kx = 1/2$$

$$\text{Or } kx = \pi/3$$

Now as  $k = 2\pi/\lambda$  we get

$$x = \lambda/6 = c/(6n) = 3 \times 10^8 / (6 \times 9.0 \times 10^5) = 55.55 \text{ m}$$