

For the circuit of Figure

(a) Find the total admittance Y_T in polar form.

The circuit contains a resistor $R = 1.2\Omega$, an inductor of reactance of $X_L = 2\Omega$ and a capacitor of reactance 5Ω in parallel.

The impedance in the different branches of the parallel circuit are

$$Z_1 = (1.2 + 0j)\Omega = 1.2\angle 0 \quad \text{gives} \quad Y_1 = 0.833 + 0j$$

$$Z_2 = (0 + 2j)\Omega = 2\angle 90^\circ \quad \text{gives} \quad Y_2 = 0 - 0.5j$$

$$Z_3 = (0 - 5j)\Omega = 5\angle -90^\circ \quad \text{gives} \quad Y_3 = 0 + 0.2j$$

Hence the total admittance of the circuit will be

$$Y = Y_1 + Y_2 + Y_3 = 0.833 - 0.3j = (0.833^2 + 0.3^2)^{1/2} \angle \tan^{-1}(-0.3/0.8333) \\ = \mathbf{0.89 \angle -19.80^\circ \Omega^{-1}}$$

(b) Draw the admittance diagram.

The admittance diagram is shown in the figure

(c) Find the value of C in microfarads and L in Henri.

The current in the circuit is

$$I = 3 \sin(377t + 60^\circ)$$

This gives the value of the angular frequency $\omega = 377 \text{ rad./s}$

As the inductive reactance $X_L = L\omega = 2\Omega$ we get

$$L = X_L / \omega = 2/377 = \mathbf{5.3 \times 10^{-3} \text{ H}} = 5.3 \text{ mH}$$

Similarly the capacitive reactance is

$$X_C = 1/C\omega = 5\Omega \text{ we get}$$

$$C = \frac{1}{\omega X_C} = \frac{1}{377 \times 5} = 5.3 \times 10^{-4} \text{ F} = 530 \times 10^{-6} \text{ F} = \mathbf{530 \mu\text{F}}$$

