

Q- (a) Draw the free-body diagram of the link at B. (b) if the spring has a stiffness of $k=800 \text{ N/m}$ and an unstretched length of 100 mm , determine the tension in cables BC and BD when the spring is held in the position shown.

Answer:

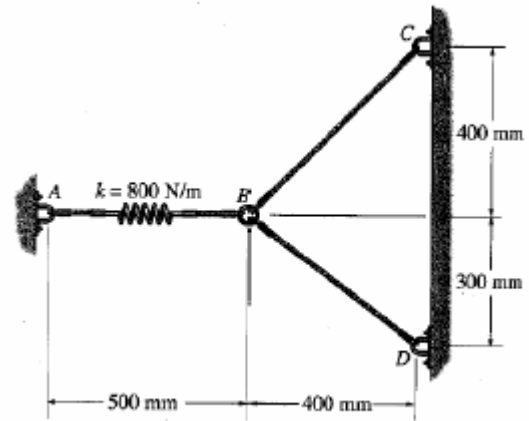
(a) The free body diagram of the link at B is shown in the figure bellow.

(b) The extension in the spring is

$$\Delta l = 500 - 100 = 400 \text{ mm} = 0.4 \text{ m}$$

hence tension in the spring is given by

$$F = K \Delta l = 800 * 0.4 = 320 \text{ N}$$

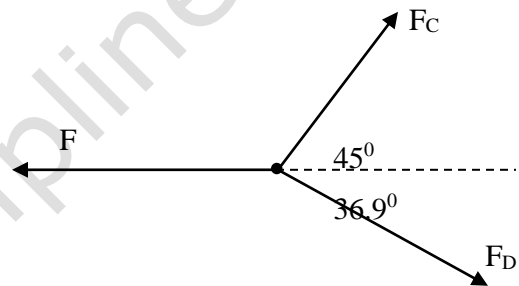


Now the geometry of the diagram shows that the force F_C is making an angle

$$\tan^{-1}(400/400) = 45^\circ$$

and the force F_D is making an angle

$\tan^{-1}(300/400) = 36.9^\circ$ with the direction opposite to the force F



Now resolving the forces F_C and F_D in the direction perpendicular and along the direction of F we have for equilibrium of point B in the direction perpendicular to F

$$F_C \sin 45^\circ - F_D \sin 36.9^\circ = 0$$

$$\text{Or } F_C * 0.707 = F_D * 0.6$$

$$\text{Or } F_C = 0.849 F_D \quad \text{----- (1)}$$

Considering equilibrium of point B along the spring force F we have

$$F_C \cos 45^\circ + F_D \cos 36.9^\circ - F = 0$$

$$\text{Or } F_C * 0.707 + F_D * 0.8 - 320 = 0$$

$$\text{Or } 0.849 * F_D * 0.707 + 0.8 F_D = 320 \quad \text{\{using equation 1\}}$$

$$\text{Gives } F_D = \mathbf{228.57 \text{ N}}$$

$$\text{And } F_C = 0.849 * F_D = \mathbf{194.05 \text{ N}}$$