

Q- Find the mesh currents and the voltage  $V_{ab}$  for the given network. The source is the current source supplying a current of 3 A.

Considering the node f we get the current in  $R_1$  as  $I_2 - I_1$  and considering node e the current through  $R_4$  is  $I_2 - I_3$ .

For mesh abefa we get (clockwise)

$$\Sigma E = E_2 = 6 \text{ V}$$

And  $\Sigma IR = (I_2 - I_3)R_4 + (I_2 - I_1)R_1 + I_2R_2$

Applying loop law for the mesh we get

$$(I_2 - I_3)R_4 + (I_2 - I_1)R_1 + I_2R_2 = 6$$

Or  $4 I_2 + 6 (I_2 - I_3) + 3 (I_2 - 3) = 6$

Or  $13 I_2 - 6 I_3 = 15$  ----- (1)

For mesh bcdeb

$$\Sigma E = E_3 = -4$$

And  $\Sigma IR = I_3R_3 - (I_2 - I_3) R_4$

Hence by loop law

$$I_3R_3 - (I_2 - I_3) R_4 = -4$$

Or  $8 I_3 - 6 (I_2 - I_3) = -4$

Or  $6 I_2 - 14 I_3 = 4$

Or  $3 I_2 - 7 I_3 = 2$  ----- (2)

Now equation (1)\*3 - equation(2)\*13 gives

$$73 I_3 = 19$$

Or  $I_3 = 19/73 \text{ A} = \mathbf{0.26 \text{ A}}$

Substituting in (2)

$$I_2 = (2 + 7*2.6)/3 = \mathbf{1.274 \text{ A}}$$

And the potential difference  $V_{ab}$  is given by

$$V_{ab} = I_2R_2 + E_2 = 1.274*4 + 6 = \mathbf{11.096 \text{ V}}$$

