

Q- A commuter train passes a station platform at a constant speed of 40 m/s. The train horn sounded at its characteristic frequency of 320 Hz. What change in frequency is detected by a person standing on the platform as the train moves past from approaching to receding? (speed of sound in air is 340 m/s)

The effect of change in the frequency of the sound heard due to relative motion between the source and the listener is called Doppler's effect.

The frequency heard by a standing listener when the source approaches to the listener is given by

$$n_1 = n \left(\frac{c}{c-v} \right)$$

Here n is the actual frequency of the source, c is the speed of sound in air and v is the velocity of approach of the source.

Hence substituting the values the frequency of the sound heard when the train is approaching is

$$n_1 = 320 \left(\frac{340}{340-40} \right) = 320 * \left(\frac{340}{300} \right) = 362.67 \text{ Hz} \quad \dots(1)$$

The frequency heard by a standing listener when the source resides away from the listener is given by

$$n_2 = n \left(\frac{c}{c+v} \right)$$

Here n is the actual frequency of the source, c is the speed of sound in air and v is the velocity of approach of the source.

Hence substituting the values the frequency of the sound heard when the train is approaching is

$$n_2 = 320 \left(\frac{340}{340+40} \right) = 320 * \left(\frac{340}{380} \right) = 286.32 \text{ Hz} \quad \dots(2)$$

Hence from equation (1) and (2) the change in frequency of the sound of the horn will be

$$\Delta n = n_1 - n_2 = 362.67 - 286.32 = 76.35 \text{ Hz}$$