

Q- Two positive, 1 nC charges are located on the x-axis. Charge Q_1 is located at the origin and charge Q_2 is located at (4, 0) which is 4 cm from the origin.

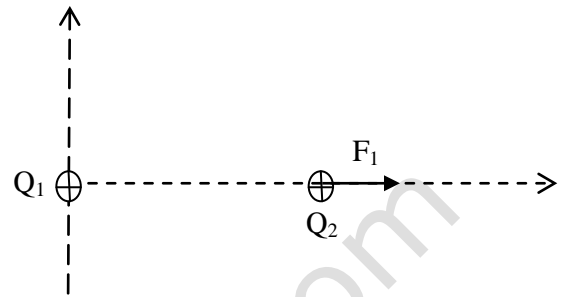
(a) Calculate the magnitude and direction of the force experienced by Q_2 due to Q_1 .

The magnitude of the force is given by Coulombs law as

$$F_1 = \frac{1}{4\pi\epsilon_0} * \frac{Q_1 Q_2}{r^2}$$

$$\text{Or } F_1 = (9 * 10^9) * \frac{(1 * 10^{-9} C) * (1 * 10^{-9} C)}{(0.04 m)^2} = 5625 * 10^{-9}$$

$$\text{Or } F_1 = \mathbf{5.625 * 10^{-6} N}$$



(b) A third charge Q_3 of 2 nC is positioned on the y-axis at (0, 4) which is 4 cm from the origin. Calculate the magnitude and direction of the total force on Q_2 due to both Q_1 and Q_3 .

The distance between Q_3 and Q_2 is

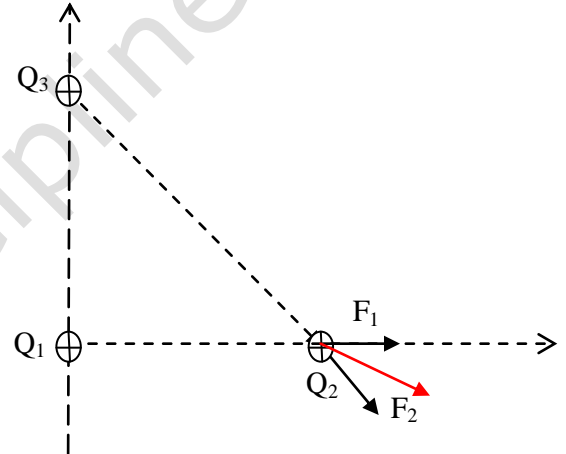
$$r = \sqrt{0.04^2 + 0.04^2} = \sqrt{0.0032} \text{ m}$$

hence magnitude of the force on Q_2 due to Q_3 is given by

$$F_2 = \frac{1}{4\pi\epsilon_0} * \frac{Q_3 Q_2}{r^2}$$

$$\text{Or } F_2 = (9 * 10^9) * \frac{(2 * 10^{-9} C) * (1 * 10^{-9} C)}{0.0032} = 5625 * 10^{-9}$$

$$\text{Or } F_2 = 5.625 * 10^{-6} \text{ N}$$



As the angle between F_1 and F_2 is 45° and they are equal in magnitude their resultant is given by

$$F = \sqrt{F_1^2 + F_2^2 + 2F_1 F_2 \cos 45^\circ}$$

$$\text{Or } F = 5.625 * 10^{-6} \sqrt{2 + 2 \cos 45^\circ} = 5.625 * 10^{-6} * 1.85 = 1.04 * 10^{-5} \text{ N}$$

As the two forces are equal in magnitude, the resultant will bisect the angle between them and hence the resultant force on Q_2 due to Q_1 and Q_3 will be $\mathbf{1.04 * 10^{-5} N}$ making angle $\mathbf{22.5^\circ}$ below the x direction.